Scheme

Announcements

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 - -Neal Stephenson, DeNero's favorite sci-fi author
- "The greatest single programming language ever designed."
 - -Alan Kay, co-inventor of Smalltalk and OOP (from the user interface video)

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> (quotient 10 2) <
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> (quotient (+ 8 7) 5)
3
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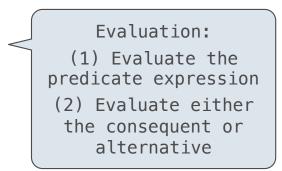
Call expressions include an operator and 0 or more operands in parentheses

(Demo)

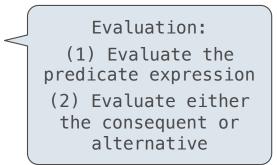
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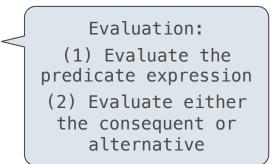
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Evaluation: (1) Evaluate the predicate expression (2) Evaluate either the consequent or alternative

> (define pi 3.14)
> (* pi 2)
6.28

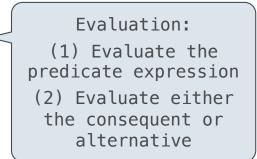
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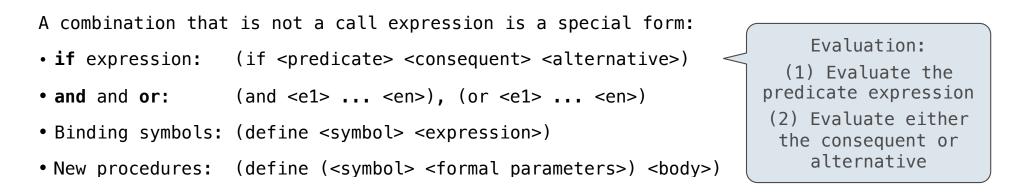
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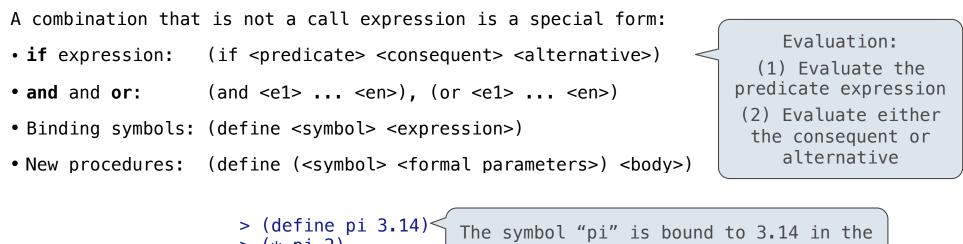
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The symbol "pi" is bound to 3.14 in the
global frame

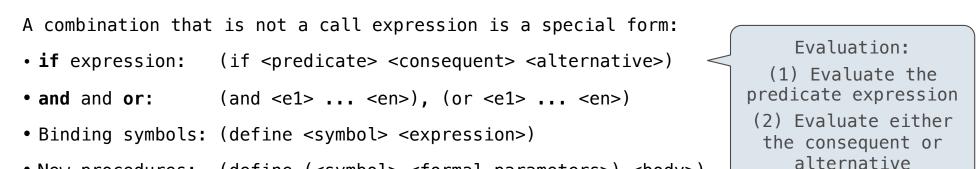
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- Binding symbols: (define <symbol> <expression>)
- New procedures: (define (<symbol> <formal parameters>) <body>)





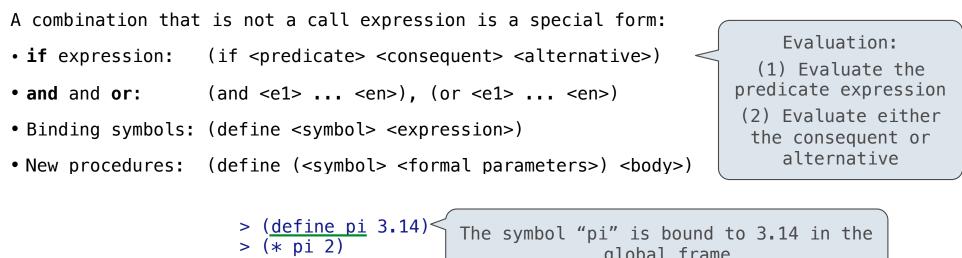


Special Forms



• New procedures: (define (<symbol> <formal parameters>) <body>)

Special Forms



Scheme Interpreters

(Demo)

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((lambda (x y z) (+ x y (square z))) 1 2 3)



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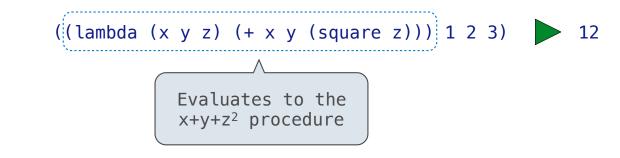
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Lists

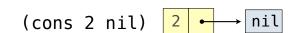
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• cons: Two-argument procedure that creates a linked list

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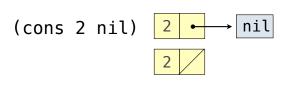
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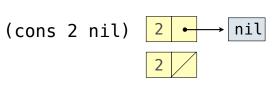


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Important! Scheme lists are written in parentheses with elements separated by spaces

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1 -	╞─→	2		
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```

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```

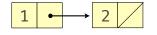
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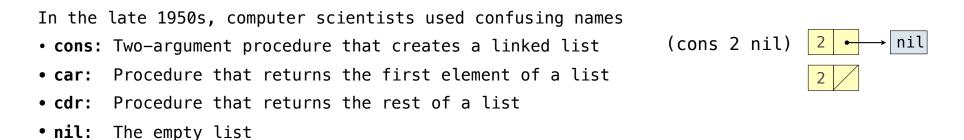
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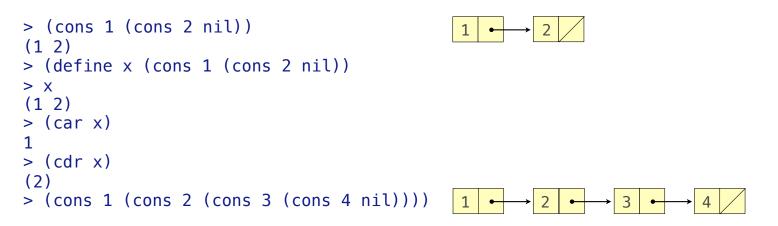
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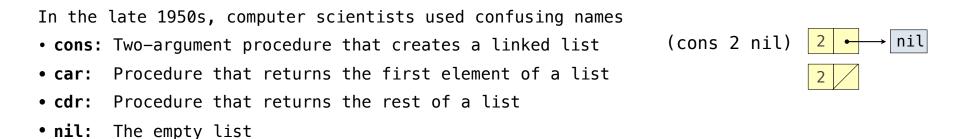
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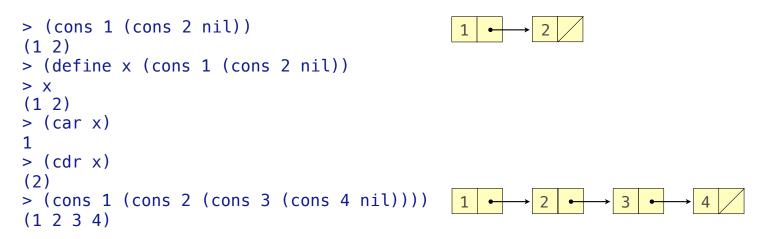
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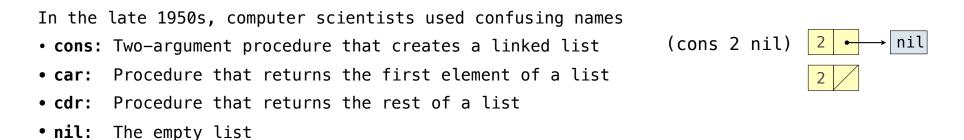
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> (cons 1 (cons 2 (cons 3 (cons 4 nil))))
```



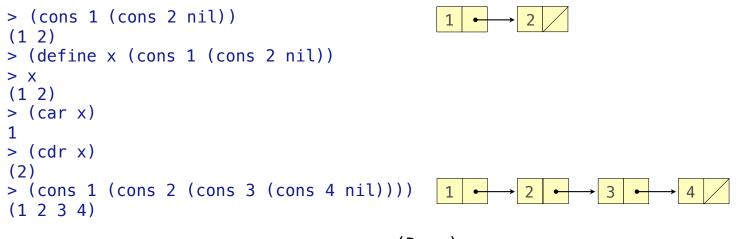








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(Demo)

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> (define a 1)

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> (define a 1)
> (define b 2)

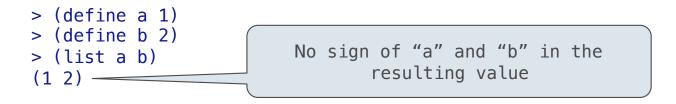
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> (define a 1)
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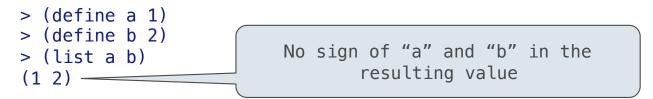
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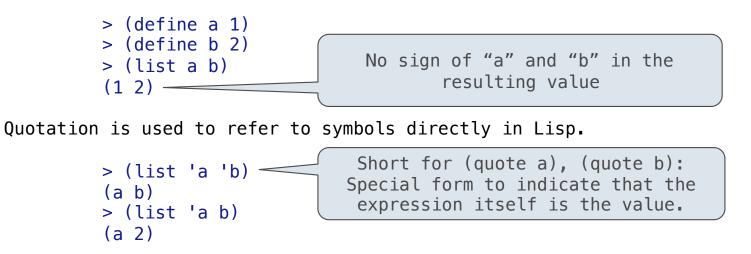
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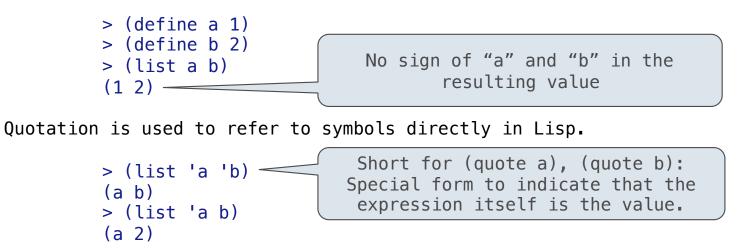
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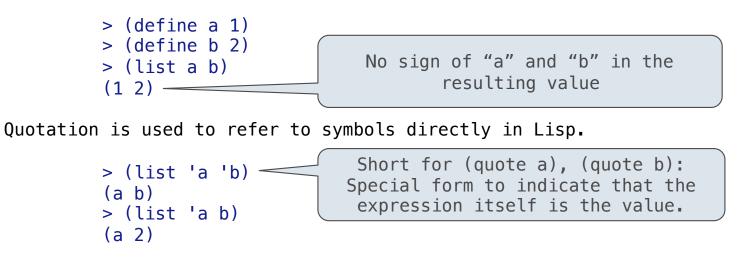
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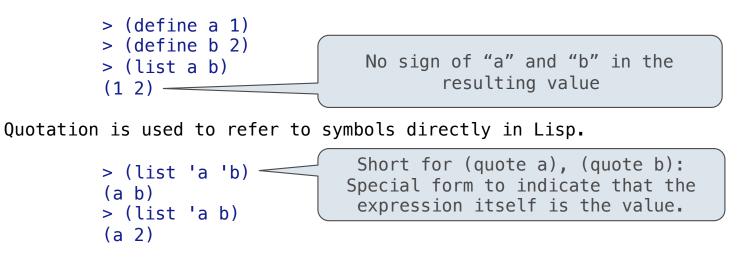
Symbols normally refer to values; how do we refer to symbols?



Quotation can also be applied to combinations to form lists.

> '(a b c)

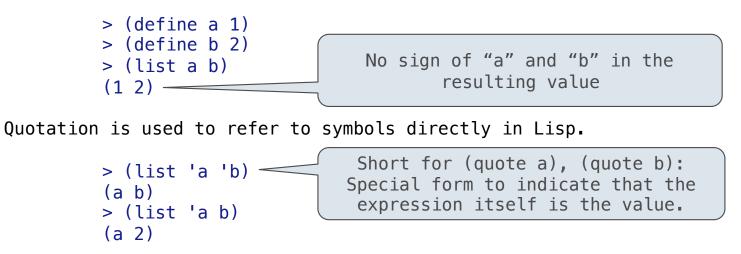
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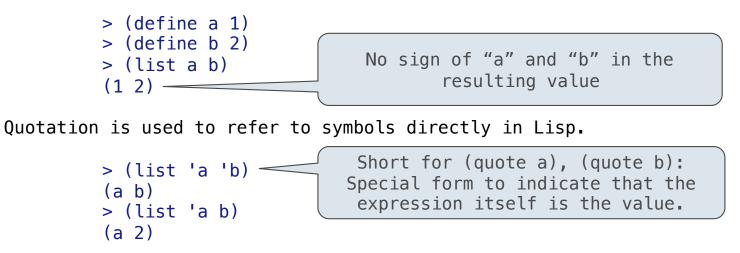
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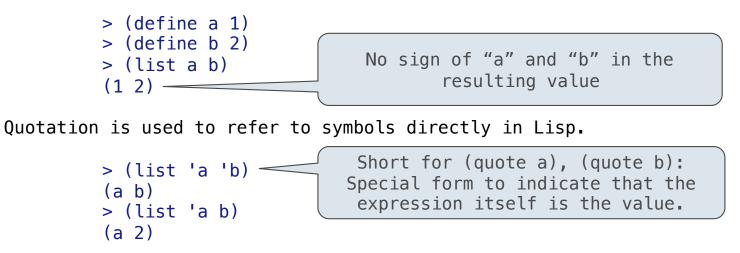
```
> '(a b c)
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> (car '(a b c))
```

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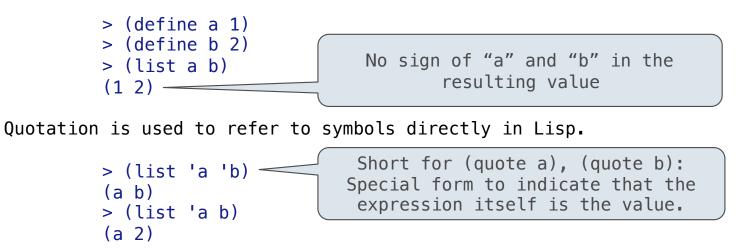
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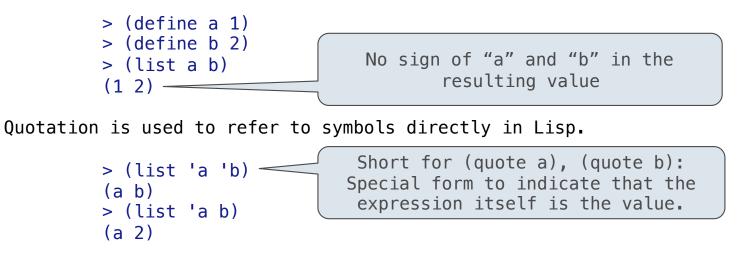
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(Demo)

Sierpinski's Triangle

(Demo)